Criticality for Alternating Branching Processes

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Abstract

This communication describes the correspondence between the models of Alternating branching processes, Controlled branching processes and Branching processes in random environment. The Control process consists of testing every particle from the n-th generation according to dying branching process during an independent random time τ_n . The random environment is generated by the sequence of random variables (δ_n, τ_n) , representing the observation and treatment times, respectively, and by the probability generating functions of the Markov branching processes stopped at the random times δ_n or τ_n .

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References

- [1] Afanasiev, V.I., Geiger, J., Kersting, G. and Vatutin, V.A. (2005). *Criticality for Branching Processes in Random Environment*. Ann. Probab., 33, 645-673.
- [2] González, M., Molina, M. and Del Puerto, I. (2002). On the class of controlled branching processes with random control functions. J. Appl. Prob., 39, 804-815.
- [3] Mayster, P. (2005). Alternating Branching Processes. J. Appl. Prob., 42, 1095-1108.